## Lechnocamps

## Assembly Language

## Session Plan




Prifysgol Metropolitan Caerdydd

University of
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pout Southwal
Prifysgol De Cymru

## Workshop Schedule

Introduction-10 minutes
Hardware - 1 hour 30 minutes

Architecture - $\mathbf{3 0}$ minutes
What is Assembly Language? - 30 minutes
Little Man Computer Tasks - 1 hour 20 minutes
Sequences (Maths GCSE) - 30 minutes

## Post-Day Questionnaires - 10 minutes

Note: These are estimated times, these will vary between classes, schools etc. so times will need to be adjusted accordingly.

Total: 4 hours 40 minutes

## Learning Outcomes

## Preparation

Ensure all computers have access to https:// peterhigginson.co.uk/LMC/
2. A small handheld whiteboard, a few blank A4 sheets, whiteboard markers, printouts for visualising activity.
3. Print out assembly language workbook, one for each student attending workshop.

1. To gain a better understanding of the fetch-decode-execute cycle.
2. To develop a strong understanding of programming in assembly language.
3. To develop understanding of sequences (mathematics GCSE topic) through assembly language programming.


## Attendee Prerequisites

1. No previous knowledge of Assembly Language programming required.

## Introduction

## Session Plan Key

In this session plan we use the following colours to differentiate the types of activities:

- Yellow - Explain. Teachers should explain the slide/example to the class.
- Green - Discuss. Teachers should start an open discussion with the class to get them to feedback some answers/ideas.
- Purple - Activity. Students are expected to complete an activity whether it be in their workbooks or on the computer, followed by a discussion of their solutions.
- Green - Introduction/Conclusion. The introduction/conclusion is also colour coded green. Teachers should hand out materials in the introduction and conclude the day and collect materials at the end.


## Introduction

Begin with introductions, and a brief explanation of the Technocamps programme, before handing out pre-day questionnaires to be filled out by the students and teacher.

## Explain: Surface Pro 5 vs. MacBook Pro 2017

Play the marketing videos of the Surface Pro 5 and the MacBook Pro 2017. Explain that the students will need to choose which of the laptops they prefer and give reasons why.

## Surface Pro vs Macbook Pro 20175

## Activity: Surface Pro 5 vs MacBook Pro 2017

Students should decide which of the two laptops they prefer and justify why, in their workbooks.

## Explain: Marketing Nonsense

The videos the students watched were full of marketing buzzwords that are designed to sell laptops and technology but which are often misleading or don't mean as much as people first think.
"This is the fastest surface pro ever" doesn't mean much if the performance increase is only .1\%
Similarly "the best retina display in a MacBook" can also be misleading and discussing how the technology works does little to show users how good a display the laptop has.

As a result, it is often better to look at the technical specifications of any piece of technology and use these to gain a better understanding of what you are actually getting.

## Explain: Internal Components

We are going to open up a desktop, show you the most important components and then install them one at a time. By the end we should have a fully functional PC.
We should also understand more about the technology inside computers and be able to make informed decisions when buying tech.

## Motherboards

## Explain: Motherboard

The motherboard is potentially the most important component with a computer. It is a PCB that houses most of the essential parts of a computer system. It is also where most of the connections between the computer and external devices are contained.

For today, we have pre-installed the motherboard. This is just to avoid damaging it when we brought it here as well as ensuring we won't short any connections later on when we power up the system.

## Extension Activity: Seating a CPU

This is an optional task if suitable for the class.
Show the class a CPU chip and then ask for two sensible volunteers to come up to the front and seat them.

## CPUs

## Explain: CPU

The CPU is the brains of the computer. On most personal computers, the CPU is housed in a single chip called a microprocessor. The CPU contains the circuitry which processes the instructions when running any computer program. The two most important things to worry about when comparing CPUs is the clock speed and the number of cores.

The clock speed of a CPU is measured in hertz $(\mathrm{Hz})$ and measures how many instructions a CPU can execute per second. It is analogous to the speed of a checkout cashier, the faster the cashier the more items it can scan a second.
A core is the part of a CPU which receives instructions and performs calculations. The more cores a CPU has, the more instructions and calculations it can perform simultaneously. The number of cores is analogous to the number of checkouts open at a super market. More checkouts open means more people can be served simultaneously.

## Discuss: Parallelisation

If you are the only person in the supermarket and you get to the checkouts, would you rather have multiple checkouts open or one checkout open with speedy Gonzales as the cashier?

Certain tasks can not be split up efficiently over multiple cores. For example, if you tried to check out your shopping over multiple tills then the time taken for all the items to be scanned may be reduced but you would still have to go to each individual till to pay and pack up into your trolley. In the long run this will take more time than just using a single checkout.
As a result, high clock speeds and multiple cores need to be used effectively in conjunction for very fast computing.

## Cooling

## Activity: Installing a Fan

Explain how the CPU fan sits directly on top of the CPU and is attached to the motherboard. Ask for two volunteers to come to the front and install the fans and the power cable for the fan.

## Explain: Cooling

The engine of a car produces a lot of heat as it burns fuel. As an engine gets hotter it starts running less efficiently and if it gets too hot it will break. To stop this from happening, cars have massive radiators to cool the engine. The radiators in turn are cooled by air flowing through them.
Many PC components work similarly. As they get hotter they work less efficiently and if they get too hot they can damage the chips inside which can break the component. This is especially relevant for CPUs and GPUs.

So we need to cool our system. This is usually done with airflow and fans but can be done using liquid cooling loops and radiators.

## Activity: Installing RAM

Show the students two RAM sticks. Explain how they are shaped with notches that fit into the RAM slots. Ask for two volunteers to come to the front and install the sticks.

## Memory

## Explain: Memory

Your computer needs to be able to store and access data so that programs can be properly run.

Cache memory is like a goldfish brain. Very small but super quick to access. Also if your system loses power or is shut down, the data stored in the cache is lost. This is known as volatile storage.
RAM, random access memory, is like sheets of paper out on your desk. You can store more data on the sheets than you could in a goldfish brain but it takes longer to access. Also if you don't file away your sheets. After using them they will be lost, similar to the goldfish brain.
Mass storage devices are things like solid state drives and hard drives. They are analogous to a file or a folder. They can hold loads of data but take much more time to access the information in them than loose sheets of paper or a goldfish brain. Most importantly they do not lose the data they contained within them after a shutdown or power loss. This is known as non-volatile storage.

Memory capacity is measured in bytes.
Having larger capacity RAM means more space for instructions that can be stored closer to the processor at any one time which reduces the amount of time spent swapping data in and out of RAM.

## Activity: Memory

Students should fill out the section in their workbooks on memory which includes volatile/non-volatile memory and memory storage amounts.

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## Explain: PCI

PCI stands for peripheral component interconnect. These are used inside PCs for connecting peripherals such as dedicated sound cards, graphic cards or wireless internet cards.

Expansion slots allow the lifetime of a system to be extended as new technology becomes available such as newer graphics cards for better visuals and dedicated ethernet cards for greater data transfer rates.

## Activity: Installing a Hard Drive

Show the students a hard drive and explain how much data it can store. Ask for two volunteers to come to the front and install it.

## Explain: SATA

The hard drive wasn't connected directly to the motherboard, there was no slot for it. Instead it was connected using a SATA cable. This cable is designed to transfer lots of data from hard drives or optical drives to the CPU.

## Comparing Technology

## Explain: //O Device Ports

Input devices such as keyboard and mouse provide a way for the user to input data into the processor and give commands.
Output devices like a monitor present the results of any processing to the user.

## Extension Explain: Overclocking

Overclocking increases the operating speed of a given component.
The target of overclocking is increasing the performance of a major chip or subsystem, such as the main processor or graphics controller, but other components, such as system memory (RAM) or system buses (generally on the motherboard), are commonly involved.

## Discuss: eMac (2005) vs. iMac Pro

Bring up the two computers and run through the slides explaining the differences in hardware. This is a good demonstration of how technology gets better.

## Activity: Compare Technology

Students should choose either the Xbox One $X$ and the Playstation 4 Pro or the HP Envy 13 (2018) and the HP Pavilion 15-cs1006na, google the chosen items and then compare their tech specs. Decide which is better and why.

## Architecture

## Explain: Architecture

Just like the architecture of a building, computer architecture is the way that a computer is designed to function in terms of hardware.
The most common architecture is known as Von Neumann architecture.
This architecture is made up of:

- CPU - Control unit, Arithmetic unit and registers
- Memory unit - RAM
- Buses - Data/address/control
- Input device - mouse, keyboard
- Output device - monitor, speakers

Von Neumann: This stores both the instructions and the data within the same memory addresses and uses the same bus for both.
Harvard: This has separate memory addresses for instructions and data meaning it can run a program and access data simultaneously.

## Activity: Von Neumann Architecture

Students to write the parts of the Von Neumann architecture next to their corresponding label in the diagram given the slides and in their workbooks.

## Architecture

## Explain: Von Neumann vs Harvard

Von Neumann architecture is more flexible than Harvard architecture. We have to decide how much memory we are dedicating to instructions and how much we are dedicating to data in Harvard architecture. If we set up or system to be able to store lots of data and few instructions, but then we are required to run a program with little data and lots of instructions, we may not be able to.
This does not occur in Von Neumann architecture as the same memory addresses are used for both data and instructions.

Harvard architecture is in theory faster than Von Neumann as it can access data and instructions simultaneously.

Harvard architecture is more costly to develop due to having two buses working simultaneously. This complicates the control unit adding to the cost.

Von Neumann architecture is used in general purpose computers that will be used for many different purposes.
Harvard architecture is used in embedded systems that perform only a few functions like a burglar alarm.

## Activity: Flexibility

Students to fill out the section on flexibility of Von Neumann architecture vs Harvard architecture in their workbooks.

## What is an Assembly Language? 14

## Explain: What Is Assembly Language?

Assembly language is a low-level programming language which uses an assembler to convert a program into machine code. Assembly languages usually use short mnemonics as instructions and each one is specific to the computer architecture and operating systems.
Assembly languages are considered to be low-level because they are very close to machine languages. They are only one step removed from a computer's machine language.

## Explain: Why Assembly?

A CPU cannot directs read source code. Different CPUs may have different architecture and each different architecture has its own machine language. This prevents direct source code to machine code translation - we need to use an assembly language to assemble the code which bridges the gap. For example, a piece of Python code assembled to run on a 64 bit Windows machine will not have the same instruction set as the Python code assembled to run on a 32 bit linux machine.

On the slides there is a simple one line program in Python. Internally it is converted to an Assembly language. If we wrote the same code directly in the assembly language we can see it only takes three instructions yet the two programs provide the same output.

Low-level languages are especially useful when speed of execution is critical or when writing software which interfaces directly with the hardware, e.g. device drivers.
Example: the Voyager space prove launched in 1977 is programmed using an old assembly language. NASA are struggling to find anyone who still has a working knowledge of the language to keep it going.

## LMC

## Activity: What Is an Assembly Language?

Students to write down what Assembly languages are and when they are useful in their workbooks.

## Explain: Little Man Computer (LMC)

LMC is a simulator which mimics von Neumann architecture.
Everything in a computers memory is data. Although programs may seem different from data, they are treated in exactly the same way: the computer executes a program, instruction by instruction.
These instructions are the 'data' of the fundamental program cycle:

1. Fetch the next instruction
2. Decode it
3. Execute it

Then the next program cycle starts which will process the next instruction. Even the location of the next instruction is just data.

## The LMC Environment

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## Explain: The LMC Environment

1. Accumulator - This is like the active memory of the simulator. The majority of our instructions will modify the contents of the accumulator.
2. Program Counter - This shows the current memory location that the processor is running.
3. Instruction and Address register - This shows which type of instruction is being used and which memory address it is being used on.
4. Memory Addresses - These are the RAM addresses which are used to store instructions and data.
5. Input Box - This is where the user inputs are stored initially before being copied to the accumulator.
6. Output Box - This is where a value is copied to from the accumulator to display to the user.

## Activity: Fill in the Blanks

Students to fill out the heading names of the environment of LMC in their workbooks.

## Explain: Input, Output, Halt

Explain the Input, Output and Halt instructions, their mnemonics and code as well as their functions and what happens after these instructions are completed.

## Visualising a Program Running

## Discuss: Visualising a Program Running

Print off the extra resources for this activity. The instructions will each be on an individual sheet.

The RAM Addresses: You will either need to use 6 boxes labelled 0 to 5 or just lay them out on a table or sellotape to a wall etc. with space for instructions underneath.

Accumulator: Get a student to be the accumulator i.e. the working working memory. This person will be handed numbers on A4 pages and will then hand these to the arithmetic unit if a calculation is required.

Arithmetic Unit: Get a student to be the arithmetic unit. This person is required to perform simple calculations when required, such as adding 1 to the counter.

Program Counter: This person can stand next to the whiteboard and update the counter each time it is given a new value by the bus.

The Bus: Again another student. For this task we simplify and just use a single bus whenever we are moving data, they must have a small handheld whiteboard to write the values on.

Input: The teacher can be the "Input Box" and decide on a value to input.
Output: The Output box can be an area on the whiteboard for writing the final outputted values.

## Visualising a Program Running

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## Activity: Visualising a Program Running

First line up the instructions in the following addresses:

## 00: INP 901 <br> 01: OUT 902 <br> 02: HLT 000

The Counter and Accumulator should begin with 0 as their number. Once this is set up we can start the activity.

## Step 1:

Bus copies value from Counter, Value is O so the bus copies the instruction from address 00 .
The bus then shows the instruction to the Control Unit (rest of the class). They decide what the instruction is and what needs to be done.
They will realise it's and Input and will need to ask for an input. In this case, the teacher can be the "user" and write a number on a blank A4 page.
The bus will then copy this to the accumulator.
This step is finished so the bus copies the value from the counter, takes it to the arithmetic unit who adds 1 and tells the bus the new value, who returns it to the counter and then the first step is finished.

In Short:

1. Bus copies Value from Counter. Value $=0$
2. Bus copies instruction from Address 00
3. Bus shows Control Unit (rest of class)
4. Control Unit decodes and asks for Input
5. Bus copies input from Input Box (Teacher)
6. Bus copies value into Accumulator. Accumulator records the value
7. Bus copies value from Counter
8. Bus takes it to Arithmetic Unit. The Arithmetic Unit adds 1
9. Bus returns to Counter who updates with new value. Counter $=1$

## Visualising a Program Running

## Activity: Visualising a Program Running

## Step 2:

1. Bus copies value from Counter. Value $=1$
2. Bus copies instruction from Address 01
3. Bus shows Control Unit (rest of class)
4. Control Unit decodes and tells bus to copy value from Accumulator to Output
5. Bus copies Value from Accumulator to Output
6. Bus copies value from Counter
7. Bus takes it to Arithmetic Unit. The Arithmetic Unit adds 1
8. Bus returns to Counter who updates with new value. Counter $=2$

## Step 3:

1. Bus copies value from Counter. Value $=2$
2. Bus copies instruction from Address 02
3. Bus shows Control Unit (rest of class)
4. Control Unit decodes and ends the program

## Discuss: What Happened?

Ask the students to summarise what the program did, what instructions were used, what did the arithmetic unit do?
Emphasise that we are copying values from the memory addresses to the bus and bus to the accumulator. i.e. at the end of the program all the instructions and data are still in the memory addresses.

## Storing, Loading, DAT

## Explain: Storing, Loading, DAT

Explain the Store, Load and DAT instructions, their mnemonics and code as well as their functions and what happens after these instructions are completed. Specifically explain the DAT instruction for reserving memory locations.

## Explain: Input \& Print a Number

The slides show a simple input and print program written in Python. An equivalent program is written in Assembly. We are going to run through this Assembly program by hand on the board to once again demonstrate how a program is executed.

## Activity: Running a Program

Convert the Assembly instructions into their corresponding codes and load them into the correct memory addresses. Then start the Counter and Accumulator at O and begin executing the instructions one at a time.

## Running a Program

## Activity: Running a Program

## Step 1:

1. Bus copies Value from Counter. Value $=0$
2. Bus copies instruction from Address 00
3. Bus shows Control Unit (rest of class)
4. Control Unit decodes and asks for Input
5. Bus copies input from Input Box (Teacher)
6. Bus copies value into Accumulator. Accumulator records the value
7. Bus copies value from Counter
8. Bus takes it to Arithmetic Unit. The Arithmetic Unit adds 1
9. Bus returns to Counter who updates with new value. Counter $=1$

## Step 2:

1. Bus copies value from Counter. Value $=1$
2. Bus copies instruction from Address 01
3. Bus shows Control Unit (rest of class)
4. Control Unit decodes and tells bus to copy value from Accumulator to Memory Address 05
5. Bus copies Value from Accumulator to Memory Address 05
6. Bus copies value from Counter
7. Bus takes it to Arithmetic Unit. The Arithmetic Unit adds 1
8. Bus returns to Counter who updates with new value. Counter $=2$

## Step 3:

1. Bus copies value from Counter. Value $=2$
2. Bus copies instruction from Address 02
3. Bus shows Control Unit (rest of class)
4. Control Unit decodes and tell bus to copy value from Memory Address 05 into Accumulator
5. Bus copies value from Address 05 into Accumulator
6. Bus copies value from Counter
7. Bus takes it to Arithmetic Unit. The Arithmetic Unit adds 1
8. Bus returns to Counter who updates with new value. Counter $=3$

## Running a Program

## Activity: Running a Program

## Step 4:

1. Bus copies value from Counter. Value $=3$
2. Bus copies instruction from Address 03
3. Bus shows Control Unit (rest of class)
4. Control Unit decodes and tells bus to copy blue from Accumulator to Output
5. Bus copies Value from Accumulator into Output
6. Bus copies value from Counter
7. Bus takes it to Arithmetic Unit. The Arithmetic Unit adds 1
8. Bus returns to Counter who updates with new value. Counter $=4$

## Step 5:

1. Bus copies value from Counter. Value $=4$
2. Bus copies instruction from Address 04
3. Bus shows Control Unit (rest of class)
4. Control Unit decodes and ends the program

## Discuss: What Happened?

Ask the students to summarise what the program did. Why were variables stored in box 05, what would happen if we had more commands, where would the variables be stored?

## Explain: How to Write Assembly Programs

Follow the slides to run through an example of how to think about constructing Assembly programs.

## Storing and Loading

## Activity: Storing and Loading 1

Disclaimer: For the following solutions in the session plan, there may be other ways of solving them and your pupils may find other some, especially when getting to the more advanced tasks.

Create a program which takes in and stores two inputs from the user and outputs the first input followed by the second input.

## Assembly Language Code

|  | INP |
| :--- | :--- |
|  | STA First |
|  | INP |
|  | STA Second |
|  | LDA First |
|  | OUT |
|  | LDA Second |
|  | OUT |
| First | HLT |
| Second | DAT |
|  |  |


| 00 | INP |  |
| :--- | :--- | :--- |
| 01 | STA | 09 |
| 02 | INP |  |
| 03 | STA | 10 |
| 04 | LDA | 09 |
| 05 | OUT |  |
| 06 | LDA | 10 |
| 07 | OUT |  |
| 08 | HLT |  |
| 09 | DAT | 00 |
| 10 | DAT | 00 |

10 DAT 00

## Activity: Storing and Loading 2

Create a program which takes and stores four inputs from the user and always outputs the third input.

## Assembly Language Code

|  | INP |
| :--- | :--- |
|  | STA First |
|  | INP |
|  | STA Second |
|  | INP |
|  | STA Third |
|  | INP |
|  | STA Fourth |
|  | LDA Third |
|  | OUT |
|  | HLT |
| First | DAT |
| Second | DAT |
| Third | DAT |
| Fourth | DAT |

00 INP
01 STA 11
02 INP
03 STA 12
04 INP
05 STA 13
06 INP
07 STA 14
08 LDA 13
09 OUT
10 HLT
11 DAT 00
12 DAT 00
13 DAT 00
14 DAT 00

## Storing and Loading

## Activity: Storing and Loading 3

Create a program which takes in three inputs and outputs them in reverse order.

## Assembly Language Code

|  |  |  |
| :---: | :---: | :---: |
|  | INP | 00 INP |
|  | STA First | 01 STA 11 |
|  | INP | 02 INP |
|  | STA Second | 03 STA 12 |
|  | INP | 04 INP |
|  | OUT | 05 OUT |
|  | LDA Second | 06 LDA 12 |
|  | OUT | 07 OUT |
|  | LDA First | 08 LDA 11 |
|  | OUT | 09 OUT |
|  | HLT | 10 HLT |
| First | DAT | 11 DAT 00 |
| Second | DAT | 12 DAT 00 |

## Explain: Addition and Subtraction

Explain the Addition and Subtraction instructions, their mnemonics and code as well as their functions and what happens after these instructions are completed.

## Activity: Addition and Subtraction 1

Create a program which takes in and stores two inputs from the user and outputs the sum of them.

|  |  | 100 Inp |
| :---: | :---: | :---: |
|  | ${ }_{\substack{\text { STP } \\ \text { TTA }}}^{\text {first }}$ | ${ }^{\text {a }}$ |
|  | ${ }_{\text {AND }}^{\text {INP }}$ First | ${ }^{02}$ |
|  |  |  |
| First |  | $\mid 06$ dar 00 |

## Addition and Subtraction

## Activity: Addition and Subtraction 2

Create a program which takes in three numbers and stores them and then outputs the sum of the first two numbers with the third subtracted.

|  | inp | 100 Inp |
| :---: | :---: | :---: |
|  | ${ }_{\text {sta }}$ First | $0^{01}$ STA 11 |
|  | ${ }_{\text {STA }} \mathrm{INP}$ second |  |
|  |  | 04 INP |
|  | STA Third | 05 STA 13 |
|  | ${ }_{\text {LDA }}^{\text {LD }}$ First |  |
|  | sub rhird | ${ }^{08} 8$ Sus 13 |
|  |  | O9 out |
|  | HLT | 10 hLT |
| st | ${ }_{\text {dar }}^{\text {Da }}$ | 111 dar 00 |
| ${ }_{\text {che }}^{\substack{\text { Second } \\ \text { Third }}}$ | ${ }_{\text {dat }}^{\text {da }}$ | 13 DAT 00 |

## Activity: Addition and Subtraction 1

Create a program which takes in a number, doubles it and then outputs the result.

Assembly Language Code

| INP |  |
| ---: | :--- |
| STA Number |  |
| ADD Number |  |
| OUT |  |
| NLT |  |
| HLT | DAT |

00 INP
01 STA 05
02 ADD 05
03 OUT
04 HLT
05 DAT 00

## Addition and Subtraction

## Activity: Addition and Subtraction 2

Create a program which takes in a number, multiplies it by eight and then outputs the result.

Assembly Language Code

|  |  |
| :--- | :--- |
|  | INP |
|  | STA First |
|  | ADD First |
|  | STA First |
|  | ADD First |
|  | STA First |
|  | ADD First |
|  | OUT |
|  | HLT |
|  | DAT |


| 00 | INP |  |
| :--- | :--- | :--- |
| 01 | STA | 09 |
| 02 | ADD | 09 |
| 03 | STA | 09 |
| 04 | ADD | 09 |
| 05 | STA | 09 |
| 06 | ADD | 09 |
| 07 | OUT |  |
| 08 | HLT |  |
| 09 | DAT | 00 |

Explain that this could be done in multiple ways. One way is to use the add command seven times i.e. First + First + . . + First.
The code above works differently. Initially it stores First, then adds First to itself. Then it "overwrites" the old First value with the new value in the accumulator $=$ First + First. It then adds the new First value to itself and stores the new value in the accumulator in the First variable. It then does one final addition with the newest updated value of First before outputting the final answer. An example with our input being five is shown below.

INP 5
STA First
ADD First
STA First
ADD First
STA First
ADD First
OUT
HLT

$$
\begin{array}{ll}
\text { Accumulator }=5 & \text { First }=0 \\
\text { Accumulator }=5 & \text { First }=5 \\
\text { Accumulator }=10 & \text { First }=5 \\
\text { Accumulator }=10 & \text { First }=10 \\
\text { Accumulator }=20 & \text { First }=10 \\
\text { Accumulator }=20 & \text { First }=20 \\
\text { Accumulator }=40 & \text { First }=20
\end{array}
$$

## Addition and Subtraction

## Activity: Addition and Subtraction Challenge

Create a program which takes in a number and multiplies it by forty.


This example highlights why we add and update a variable in multiplication. By updating the variable we have reduced the 39 lines of "ADD First" to only 17 total lines of code which is much more efficient. Again an example is shown below with our input being seven.

INP 7
STA First
STA Second
ADD First
STA First
ADD First
STA First
ADD Second
STA First
ADD First
STA First
ADD First
STA First
ADD First
OUT
HLT

Accumulator $=7$
Accumulator $=7$
Accumulator $=7$
Accumulator $=14$
Accumulator $=14$
Accumulator $=28$
Accumulator $=28$
Accumulator $=35$
Accumulator $=35$
Accumulator $=70$
Accumulator $=70$
Accumulator $=140$
Accumulator $=140$
Accumulator $=280$

First $=0$
First $=7$
First $=7$
First $=7$
First $=14$
First $=14$
First $=28$
First $=28$
First $=35$
First $=35$
First $=70$
First $=70$
First $=140$
First $=140$

Second $=0$
Second $=0$
Second $=7$
Second $=7$
Second $=7$
Second $=7$
Second $=7$
Second $=7$
Second $=7$
Second $=7$
Second $=7$
Second $=7$
Second $=7$
Second $=7$

## Addition and Subtraction

## Explain: Branch Always

At this point you should give each student a copy of the cheat sheet so they can see the command tables. Then continue by explaining the Branch Always instruction, its mnemonic and code as well as its function and what happens after this instruction has been completed.

## Activity: Looping 1

Create a program which allows the user to input numbers indefinitely and outputs each number.

## Assembly Language Code

|  |  |
| :---: | :---: |
| ${ }_{\text {BRA }}^{\text {OUT }} 00$ | ${ }^{01}$ OUP |

## Activity: Looping 2

Create a program which allows the user to input numbers indefinitely and outputs the running total after each entry.

|  |  |  |
| :---: | :---: | :---: |
|  | ${ }_{\text {ADP }}^{\text {INP }}$ fotal | $\left.\right\|_{0} ^{00}$ ONP |
|  | OUT | ${ }^{02}$ OUT |
|  | ${ }_{\text {BRA }}$ STR | ${ }^{0}$ |
| tal | dar 0 | $\mid 05 \mathrm{dar} 00$ |

## Comparing Values

## Explain: Branch If Zero or Positive

Explain the conditional Branching instructions, their mnemonics and code as well as their function and what happens after these instructions are completed.

## Explain: Comparing Values in Assembly

In LMC we don't have "if statements" like we have in Python or other languages for comparing. The only way to branch based on a condition is to do a subtraction and then branch based on the result. For example, if we want to output the biggest number of 2 and 5 , we would take 2 , subtract 5 and then check if the answer is positive (or zero) or negative. Here's an example:


## Conditional Branching

## Activity: Conditional Branching 1

Create a program which allows the user to input two numbers and outputs the smallest number. Hint: if you do $a-b$ and the number is positive, then $a$ is bigger than b .

## Assembly Language Code

| INP | 00 INP |
| :---: | :---: |
| STA First | 01 STA 12 |
| INP | 02 INP |
| STA Second | 03 STA 13 |
| SUB First | 04 SUB 12 |
| BRP OutPutSecond | 05 BRP 09 |
| LDA First | 06 LDA 12 |
| OUT | 07 OUT |
| HLT | 08 HLT |
| OutPutSecond LDA Second | 09 LDA 13 |
| OUT | 10 OUT |
| HLT | 11 HLT |
| First DAT | 12 DAT 00 |
| Second DAT | 13 DAT 00 |

## Activity: Conditional Branching 2

Create a program which repeatedly allows the user to input two numbers and checks if they are equal. Only output the number if they are equal.

## Assembly Language Code

|  | INP |
| :---: | :---: |
|  | STA First |
|  | INP |
|  | SUB First |
|  | BRZ Equal |
|  | BRA 00 |
| Equal | LDA First |
|  | OUT |
|  | BRA 00 |
| First | Dat |

00 INP
01 STA 09
02 INP
03 SUB 09
04 BRZ 06
05 BRA 00
06 LDA 09
07 OUT
08 BRA 00
09 DAT 00

## Conditional Branching

## Activity: Conditional Branching 3

Create a program which repeatedly takes in inputs and only outputs them if they are zero.


## Activity: Conditional Branching 4

Create a program which outputs everything except zeroes.

## Assembly Language Code

INP<br>BRZ Num1=0<br>OUT

00 INP
01 BRZ 03

Num1 $=0$ BRA 00

02 OUT
03 BRA 00

## Conditional Branching

## Activity: Conditional Branching Challenge

## Create a program which allows the user to input two numbers and outputs the multiplication of the two numbers.

## Assembly Lancuage Code

|  | INP |
| :--- | :--- |
|  | STA Total |
|  | STA First |
|  | INP |
|  | SUB One |
|  | STA Second |
|  | LDA Total |
|  | ADD First |
|  | STA Total |
|  | LDA Second |
|  | SUB One |
|  | STA Second |
|  | BRZ Output |
|  | BRA Loop |
| Output | LDA Total |
|  | OUT |
|  | BRA 00 |
| One | DAT 1 |
| Total | DAT |

## Sequences (Mathematics GCSE) 34

## Explain: Sequences

In order to calculate the equation for a given sequence of numbers we must first look at the difference between them e.g.
Index term:

$$
\begin{aligned}
& 1 \begin{array}{ll}
1 & 3
\end{array} 4 \quad 5 \ldots \\
& +2+2+2+2
\end{aligned}
$$

Number:

$$
3,5,7,9,11 \ldots
$$

So the difference between each number is +2 . So the number in front of the nth term in our equation must be 2 i.e. $\mathbf{2 n}$. The final step is to check if we need to add or subtract from our $\mathbf{2 n}$.

If we try inserting the index term into our nth term equation $\mathbf{2 n}$ does the answer match up correctly? $2 \times 1=2$
So what should we add to correct this? +1
Therefore our equation must be : $\mathbf{2 n + 1}$
Does it work for all the values?

## Discuss: Another Example

Run through the additional example together as a class, getting the students to answer each question to calculate the correct equation.

## Sequences (Mathematics GCSE) 35

## Activity: Sequences

For the following sequences:
a. Write out the nth term equation.
b. Calculate the 20th term of the sequence.

1. $7,8,9,10,11$
2. $3,6,9,12,15$
3. $12,17,22,27,32$
4. $-6,-2,2,6,10$
5. 3, -3, -9, -15, -21
6. a. Write out the first 5 terms of the sequence given by $3 n-7$.
b. Calculate the 15th term of the sequence.

## Sequences (Mathematics GCSE)

## Discuss: Solutions

1a) $n+6$
1b) $20+6=26$
2a) $3 n$
2b) $3 \times 20=60$
3a) $5 n+7$
3b) $(5 \times 20)+7=107$
4a) $4 n-10$
4b) $(4 \times 20)-10=70$
5a) $-6 n+9$
5b) $(-6 \times 20)+9=-111$
6a) $-4,-1,2,5,8$
6b) $(3 \times 15)-7=38$

## Activity: Implementing Sequences in LMC

Students to implement this nth term equation in LMC to produce the first 5 terms in the sequence: $5,6,7,8,9 \ldots$

Students should plan how to write this program in pairs. Encourage them to think about:
What is the nth term equation?
Would you need to use a loop?
What other variables would you need?
Hint: You will need to be adding or subtracting by 1, how could you implement this?

## Sequences in LMC

## Discuss: Implementing Sequences in LMC

Ask the students how they attempted to create the sequence. Did any of them use a loop? Did they set any variables? If so, what were they?

## Explain: The First Value

To get the first result we need to load the first index term =1, add 4 to it and then output it.

We always add 4 in our nth term equation so should store 4 as a variable called number?

We also need to define a variable so we know which index term we are inserting into


## Sequences in LMC

## Explain: Looping for More Values

We need to add one to the term variable before we calculate the next number in our sequence. To do this we define a variable called one which we add to the term variable. We use a loop to repeat the previous calculations and output each new number in the sequence.


Increase the current term by one and store it again.

## Explain: Only Outputting the First 5 Values

If we want to stop the loop after 5 values have been output we need to compare our index term variable to a limit. Once our term reaches the same value as the limit, we halt the program.

Check if the term and limit are the same, if so jump to the HLT instruction.

LDA term
ADD number2 OUT
LDA term
ADD one
STA term SUB limit BRZ StopProgram BRA 00
StopProgram HLT term DAT 1
one number 2 limit

| LDA term |
| :---: |
| ADD number2 |
| OUT |
| LDA term |
| ADD one |
| STA term |
| $\left(\begin{array}{ll}\text { SUB } & \text { limit } \\ \text { BRZ } & \text { StopProgram } \\ \text { BRA } & 00\end{array}\right)$ |
| StopProgram HLT |
| term DAT 1 |
| one DAT 1 |
| number2 DAT 4 |
| limit DAT 6 |

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Note: The variable limit is set to 6. Is this correct?
Yes, we increment the loop counter before checking how many times we have looped

## Sequences in LMC

## Activity: Creating Your Own Sequences

You can now use this code as a starting point for creating your own sequences. What would we change to make the sequence $n+8$ for example?

The students should answer the question in their workbooks and try running the code in LMC to see if they are correct.

$$
\begin{aligned}
& n-7 \\
& 2 n+4 \\
& 2 n-6 \\
& 3 n+8 \\
& 8 n-3
\end{aligned}
$$

|  | LDA term | 00 |
| :---: | :---: | :---: |
|  | ADD number2 | 01 |
|  | OUT | 02 |
|  | LDA term | 03 |
|  | ADD one | 04 |
|  | STA term | 05 |
|  | SUB limit | 06 |
|  | BRZ StopProgram | 07 |
|  | BRA 00 | 08 |
| StopProgr | ram HLT | 09 |
| term D | DAT 1 | 10 |
| one D | DAT 1 | 11 |
| number2 D | DAT 4 | 12 |
| limit D | DAT 6 | 13 |

## Discuss: Solutions

For these tasks, the number before the $n$ is achieved by repeating an "ADD term" instruction the respective amount of times. So for $2 n+4$ the only thing we would do to change the code is insert and ADD term after LDA term, this is then doubling our term from 1 to 2 , hence giving us 2 n .

Code for $2 n+4$ :
Assembly Language Code

|  | LDA term |  |
| :--- | :--- | :--- |
|  | ADD term |  |
|  | ADD number2 |  |
|  | OUT |  |
|  | LDA | term |
|  | ADD one |  |
|  | STA | term |
|  | SUB | limit |
|  | BRZ | StopProgram |
|  | BRA | 00 |
| StopProgram | HLT |  |
| term | DAT | 1 |
| one | DAT | 1 |
| number2 | DAT | 4 |
| limit | DAT | 6 |


| 00 | LDA | 11 |
| :--- | :--- | :--- |
| 01 | ADD | 11 |
| 02 | ADD | 13 |
| 03 | OUT |  |
| 04 | LDA | 11 |
| 05 | ADD | 12 |
| 06 | STA | 11 |
| 07 | SUB | 14 |
| 08 | BRZ | 10 |
| 09 | BRA | 00 |
| 10 | HLT |  |
| 11 | DAT | 01 |
| 12 | DAT | 01 |
| 13 | DAT | 04 |
| 14 | DAT | 06 |

## Sequences in LMC

## Discuss: Solutions

2n-6:
Number of "ADD term" instructions =1
number2 $=-6$
$3 n+8:$
Number of "ADD term" instructions $=2$
number2 $=-3$
$8 n-3$ :
Number of "ADD term" instructions $=7$
number2 $=-3$
In order to find a given nth term, we only need to change the limit to $n+1$. So if we wanted the 20th term in a sequence, we would just change the limit to 21 and write the final value given.

## Advanced LMC

## Activity: Advanced LMC 1

Create a program which takes in input and outputs the positive value. If the input is negative, you output the positive so if we input -3 we would output 3 .

## Assembly Language Code

INP
BRP Positive
STA First
SUB First
SUB First
Positive OUT
BRA 00
First DAT

00 INP
01 BRP 05
02 STA 07
03 SUB 07
04 SUB 07
05 OUT
06 BRA 00
07 DAT 00

## Activity: Advanced LMC 2

Create a program which takes and input, outputs that value and then counts down and outputs every value until it reaches 0 (or counts up to 0 if the value input is negative.

## Assembly Language Code

INP
Output OUT
BRP Positive
ADD One
BRA CheckIfZero
Positive SUB One
CheckIfZero BRZ FinalOutput
BRA Output
FinalOutput OUT
One BRA 00
DAT 1

00 INP
01 OUT
02 BRP 05
03 ADD 10
04 BRA 06
05 SUB 10
06 BRZ 08
07 BRA 01
08 OUT
09 BRA 00
10 DAT 01

## Advanced LMC

## Activity: Advanced LMC 3

Create a program which takes two inputs and checks if they have the same sign (both positive or both negative). If they have the same sign output a zero, otherwise output a 1.

## Assembly Language Code

INP<br>BRP Positive<br>LDA Zero<br>STA 98<br>BRA nextInput<br>Positive LDA One<br>STA 98<br>nextInput INP<br>BRP Positive2<br>LDA Zero<br>STA 99<br>BRA Subtract<br>Positive2 LDA One<br>STA 99<br>Subtract SUB 98<br>BRZ SameSign<br>LDA One<br>SameSign OUT<br>BRA 00<br>Zero DAT 0<br>One DAT 1

$\begin{array}{lll}00 & \text { INP } \\ 01 & \text { BRP } & 05 \\ 02 & \text { LDA } & 19 \\ 03 & \text { STA } & 98 \\ 04 & \text { BRA } & 07 \\ 05 & \text { LDA } & 20 \\ 06 & \text { STA } & 98 \\ 07 & \text { INP } & \\ 08 & \text { BRP } & 12 \\ 09 & \text { LDA } & 19 \\ 10 & \text { STA } & 99 \\ 11 & \text { BRA } & 14 \\ 12 & \text { LDA } & 20 \\ 13 & \text { STA } & 99 \\ 14 & \text { SUB } & 98 \\ 15 & \text { BRZ } & 17 \\ 16 & \text { LDA } & 20 \\ 17 & \text { OUT } & \\ 18 & \text { BRA } & 00 \\ 19 & \text { DAT } & 00 \\ 20 & \text { DAT } & 01\end{array}$

## Advanced LMC

## Activity: Advanced LMC 4

Create a program which takes two inputs and returns the remainder if you divided the first by the second. (Don't worry about negative numbers, but zero by a number and dividing a number by zero should be considered.)

## Assembly Language Code



## Explain: The Fibonacci Sequence

Note: The Fibonacci sequence is made by adding the previous number to the current one, starting with 1:

$$
\begin{array}{r}
\mathbf{1} \\
0+1=\mathbf{1} \\
1+1=\mathbf{2} \\
2+1=\mathbf{3} \\
3+2=\mathbf{5} \\
5+3=\mathbf{8}
\end{array}
$$

## Very Advanced LMC

## Activity: Very Advanced LMC

Create a program which takes in an input and outputs all of the numbers in the Fibonacci sequence up to that input number. The Fibonacci sequence is 1 , $1,2,3,5,8,13,21$
You can set one variable to 1 at the beginning. No cheating!


